Review

Solubility Data of Potential Salts in the MgO-CaO-SO$_2$-H$_2$O-O$_2$ System for Process Modeling

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Abstract: This review studies unwanted precipitation reactions, which can occur in SO$_2$ absorption processes using a magnesium hydroxide slurry. Solubility data of potential salts in the MgO-CaO-SO$_2$-H$_2$O system are evaluated. The reviewed data can serve as a reliable basis for process modeling of this system used to support the optimization of the SO$_2$ absorption process. This study includes the solubility data of MgSO$_3$, MgSO$_4$, Mg(OH)$_2$, CaSO$_3$, CaSO$_4$, and Ca(OH)$_2$ as potential salts. The solubility is strongly dependent on the state of the precipitated salts. Therefore, this review includes studies on the stability of different forms of the salts under different conditions. The solubility data in water over temperature serve as a base for modeling the precipitation in such system. Furthermore, influencing factors such as pH value, SO$_2$ content and the co-existence of other salts are included and available data on such dependencies are reviewed. Literature data evaluated by the International Union of Pure and Applied Chemistry (IUPAC) are revisited and additional and newer studies are supplemented to obtain a solid base of accurate experimental values. For temperatures higher than 100 °C the available data are scarce. For a temperature range from 0 to 100 °C, the reviewed investigations and data provide a good base to evaluate and adapt process models for processes in order to map precipitations issues accurately.

Keywords: solid-liquid phase equilibria; precipitation; SO$_2$ absorption; magnesium hydroxide slurry; sulfates; sulfites; hydroxides

1. Introduction

The removal of SO$_2$ from exhaust gas using an absorptive magnesium-based slurry is a well-established method to control SO$_2$ emissions and simultaneously recover Sulfur as a resource of further usage. The pulp production industry using magnesium bisulfite as cooking liquor can ensure a nearly full chemical recovery if applying the absorption process in an optimized way.

After combustion, magnesium oxide is recovered from the ash, hydrated to magnesium hydroxide, and serves subsequently as absorbent. The absorption of SO$_2$ from the exhaust gas with hydrated magnesium oxide forms magnesium bisulfite, which serves again as cooking liquor. Equations (1)–(3) show the simplified reactions leading to the recovered cooking liquor.

\[
\begin{align*}
  \text{MgO} + \text{H}_2\text{O} & \rightarrow \text{MG(OH)}_2 \\
  \text{MG(OH)}_2 + \text{SO}_2 & \rightarrow \text{MgSO}_3 + \text{H}_2\text{O} \\
  \text{MgSO}_3 + \text{SO}_2 + \text{H}_2\text{O} & \rightarrow \text{Mg(HSO}_3)_2 
\end{align*}
\]

This process allows the full reuse of required chemicals leading to a nearly closed-loop process control.

However, besides the intended reactions, unwanted precipitation reactions can occur under unideal process conditions. The precipitation of salts in the system highly influences the efficiency of the process. A high precipitation rate causes chemical loss as the...
precipitated salts will be washed out in a regular cleaning step rather than recycled in the process [1]. Uncontrolled precipitation of salts therefore means interruption of the closed-loop process leading to an increased usage of fresh chemicals and to more frequent cleaning operations. This challenges not only the ecological footprint but also the economic feasibility.

To prevent precipitation and provide a cleaner and more efficient production, it is essential to understand the precipitation reactions in the system. Advanced process modeling can help in optimizing process conditions. A model, which covers the complex matter of precipitation reactions in electrolyte systems, requires the inclusion of all necessary dependencies sufficiently. Reliable literature data are of vital importance to ensure accuracy of the developed model. This makes a comprehensive review of available solubility data in the literature necessary.

While MgO, SO\textsubscript{2} and H\textsubscript{2}O are process elements, CaO and O\textsubscript{2} can influence the reaction system as non-process elements. CaO can enter the process with process water and can consequently contribute to precipitation issues in the system. O\textsubscript{2} enters the process as remaining oxygen in the exhaust gas stream and can influence precipitation due to oxidation. To provide a comprehensive understanding of the precipitation process in the system, this review studies the solubility of salts in the MgO-CaO-SO\textsubscript{2}-H\textsubscript{2}O-O\textsubscript{2} system based on available literature data.

The following covers a comprehensive review of available solubility data for MgSO\textsubscript{3}, CaSO\textsubscript{3}, MgSO\textsubscript{4}, CaSO\textsubscript{4}, Mg(OH)\textsubscript{2} and Ca(OH)\textsubscript{2} as potential salts in the system. One major source for solubility data is the solubility data series of the International Union of Pure and Applied Chemistry (IUPAC) [2,3]. However, not all potential salts are covered in these evaluations. Therefore, this review includes additional data and also complements the data with newer studies to comprehensively review the state of the art of available solubility data. Furthermore, correlations describing the solubility reported in the literature are included and reviewed.

Based on the data, this paper recommends strategies for sufficiently accurate modeling of the precipitation. Although original data are partially given in molar units, this review gives all solubility data in g/100 g to provide consistency throughout the review.

2. Chemical System and Precipitation of Salts

Figure 1 visualizes simplified the chemical system leading to the formation and precipitation of sulfites, sulfates, and hydroxides in the studies system.

![Figure 1. Chemical system leading to precipitations in the MgO-CaO-H\textsubscript{2}O-SO\textsubscript{2}-O\textsubscript{2} system.](image)

SO\textsubscript{2} and O\textsubscript{2} from the gas phase dissolve into the liquid phase according to the Vapor-Liquid-Equilibrium (VLE). The presence of Mg\textsuperscript{2+} from dissolved Mg(OH)\textsubscript{2} (see Section 2.5) and the presence of SO\textsubscript{3}—from dissolved SO\textsubscript{2} in the liquid phase lead to the formation
of MgSO$_3$, Mg(OH)$_2$ and MgSO$_3$ are intended products of the main process reactions (compare Equations (1)–(3)). Ca(OH)$_2$ and CaSO$_3$ are formed in the presence of CaO as a non-process-element in the same manner. The presence of oxygen in the exhaust gas can lead to oxidation of sulfites and the formation of MgSO$_4$ and CaSO$_4$ [4]. Mg(OH)$_2$, Ca(OH)$_2$, MgSO$_3$, CaSO$_3$, MgSO$_4$ and CaSO$_4$ can precipitate in the system according to the Solid-Liquid-Equilibrium (SLE). The following focuses on the solubility of these potential salts.

Sulfites and Sulfates precipitate as different hydrates depending on process conditions [2]. The solubility of the hydrate forms can differ greatly. Understanding the stability behavior of these hydrate forms is therefore of great practical interest when developing a reliable process model.

2.1. Magnesium Sulfite (MgSO$_3$)

Equation (4) shows the solution equilibrium of MgSO$_3$.

$$\text{MgSO}_3 \text{(s)} + x \times \text{H}_2\text{O (aq)} \leftrightarrow \text{Mg}^{2+} \text{(aq)} + \text{SO}_3^{2-} \text{(aq)} + x \times \text{H}_2\text{O (aq)}$$

Lutz’s evaluation in the Solubility Data Series of IUPAC reported that the stable hydrate form of MgSO$_3$ at temperatures lower than 37.85 °C is hexahydrate (MgSO$_3$$^\ast$$6\text{H}_2\text{O}$). At temperatures higher than 37.85 °C it is trihydrate (MgSO$_3$$^\ast$$3\text{H}_2\text{O}$) [2]. This report is based on the studies of Hagisawa, Okabe et al., Pinaev et al., and Lutz et al. [5]. However, a slow conversion rate from the metastable hexahydrate to trihydrate leads to the establishment of a metastable solubility equilibrium and the crystallization of hexahydrate even at temperatures higher than 37.85 °C [6,7].

The conversion of hexahydrate to trihydrate is a pH and temperature depending process. Steindl et al. monitored the conversion using Raman Spectroscopy [1]. While at a temperature of 68 °C the conversion was completed after around 50 min, at a temperature of 53 °C the conversion was completed after around 580 min. The studies also showed an increasing conversion time with increasing starting pH value [1]. Following Steindl et al. a low pH value and high temperatures enhance therefore the conversion of hexahydrate to trihydrate. At temperatures higher than 40 °C, magnesium hexahydrate has a higher solubility than trihydrate (see Figure 2). Preventing the conversion of hexahydrate to trihydrate is therefore of practical interest to lower precipitation.

2.1.1. Solubility of MgSO$_3$ Hydrates in Water

Figure 2 shows solubility data of magnesium hexa- and trihydrate in water. The data found in the literature are mutually in very good agreement. The studies of Hagisawa and Markant were evaluated by Lutz in the IUPAC Solubility data series [2,5,8,9]. The data captured by Söhnel and Rieger and by Lowell et al. match those studies very well [6,8].

While the solubility of magnesium hexahydrate is increasing with temperature, the solubility of trihydrate is decreasing with temperature. This indicates that the dissolution of trihydrate is exothermic whereas the dissolution of hexahydrate is endothermic. Nyvlt was able to describe the temperature dependency of the solubility by correlating the data of Lowell, leading to the following equations with $x$ being the molar fraction and $T$ the temperature in K [10]:

$$\ln x_{\text{MgSO}_3^{\ast}6\text{H}_2\text{O}} = -82.918 - \frac{2668.11}{T} - 28.268 \log T$$

$$\ln x_{\text{MgSO}_3^{\ast}3\text{H}_2\text{O}} = -79.595 - \frac{4179.381}{T} - 25.435 \log T$$
The data found in the literature are mutually in very good agreement. The studies of Hagisawa and Markant were evaluated by Lutz in the IUPAC Solubility data series [2,5,8,9]. The data captured by Söhnel and Rieger and by Lowell et al. match those studies very well [6,8].

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$$\ln x_{\text{MgSO}_3 \cdot 3\text{H}_2\text{O}} = -79.595 - 4179.381 \frac{T}{T - 25.435 \log T}$$

The plot of these equations in Figure 2 shows a good correlation with existing literature data for trihydrate and hexahydrate at temperatures up to 60 °C. The correlation shows an increasing deviation from data points at higher temperatures.

The solubility of the two hydrate forms have an inverse dependency on temperature and the conversion times can be long. Consequently, occurring precipitation in the system is highly dependent on residence time and process conditions. While the given data provide a solid base for modeling purposes, a critical review of each given case is necessary to cover the change in solubility accurately.

However, the solubility of MgSO$_3$ in the MgO-CaO-SO$_2$-H$_2$O-O$_2$ system is not solely a function of temperature.

2.1.2. Influence of SO$_2$ on Solubility of MgSO$_3$ Hydrates

The solubility of MgSO$_3$ increases with increasing SO$_2$ content in the solution [2]. Figure 3 shows experimental data as well as a correlation of literature data of the solubility of magnesium sulfate over the SO$_2$ content in the solution at 25 °C [2,11].

Lutz recommends describing the change in solubility with the presence of SO$_2$ by following correlation with $S$ being the Solubility of MgSO$_3$ in mol/kg and $b$ the molality of SO$_2$ in mol/kg [2]:

$$S_{\text{MgSO}_3} = 0.0347 + 0.4885 \times b_{\text{SO}_2}$$

Figure 3 shows the good agreement of this correlation with the available experimental data by Conrad and Brice. The increasing solubility with an increasing SO$_2$ content can be explained with the formation of Mg(HSO$_3$)$_2$ (see Equation (3)). Several studies recorded an increasing amount of total dissolved magnesium sulfite with increasing amount of Mg(HSO$_3$)$_2$ in the MgSO$_3$-Mg(HSO$_3$)$_2$-H$_2$O system [2].
2.1.2. Influence of SO$_2$ on Solubility of MgSO$_3$ Hydrates

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Figure 3. Solubility of MgSO$_3$ over total SO$_2$ content in the solution [2, 11].

Lutz recommends describing the change in solubility with the presence of SO$_2$ by the following correlation with $S$ being the solubility of MgSO$_3$ in mol/kg and $b$ the molality of SO$_2$ in mol/kg [2]:

$$ S_{MgSO_3} = 0.0347 + 0.4885 \times b_{SO_2} $$

(7)

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2.1.3. Influence of MgSO$_4$ on Solubility of MgSO$_3$ Hydrates

Several authors reported the influence of MgSO$_4$ on the solubility of MgSO$_3$. Figure 4 shows the solubility of MgSO$_3$ hexahydrate over the MgSO$_4$ content in the solution and Figure 5 the solubility of MgSO$_3$ trihydrate respectively. The presence of MgSO$_4$ may also influence whether trihydrate or hexahydrate is formed as stable form [6, 8]. Pinaev explains this by the effect of MgSO$_4$ on the solution temperature and viscosity [8]. However, there are not enough studies found to confirm and characterize this influence sufficiently.

The data of Kovachev et al., 1970, Pinaev 1964 and Nvylt et al., 1977 are taken from the IPUAC solubility data series [2]. The experimental data for trihydrate and hexahydrate are in relatively good agreement with each other. All studies report an increase in solubility with increasing MgSO$_4$ content. Kovachev et al. covered the widest range of MgSO$_4$ content. The study covers the whole range of MgSO$_4$ content in which only MgSO$_3$ hydrates precipitate. At higher MgSO$_4$ contents than plotted in Figures 4 and 5, MgSO$_4$ hydrates precipitated besides MgSO$_3$ hydrates [2].

The data of Kovachev et al. show a maximum in solubility of MgSO$_3$ at MgSO$_4$ content of around 13 to 17 g per 100 g for trihydrate as well as for the hexahydrate [2]. The data for hexahydrate reported by Pinaev indicate as well that the solubility stabilizes when reaching a certain amount of MgSO$_4$ [2]. Lowel et al. present a graph showing the dependency between MgSO$_4$ content and the solubility of MgSO$_3$ hexahydrate based on values reported by Pinaev and McGlamery et al. [8].

The data of Söhnel and Kovachev et al. show that the effect of the presence of MgSO$_4$ on the solubility of MgSO$_3$ trihydrate is smaller for lower temperatures [2, 6].

Nývlt correlated literature data to describe the influence of MgSO$_4$ on the solubility of hexahydrate with the following equation with $S$ being the Solubility in kg/kg H$_2$O and $x_{MgSO_4}$ being the content of MgSO$_4$ in kg/kg H$_2$O [10]:

$$ S_{MgSO_3} = \left( 1 + 8.54 \times x_{MgSO_4} - 28.92 \times x_{MgSO_4}^2 \right) \times S_{MgSO_3 \text{ in water}} $$

(8)
Figure 4 shows the plot of this correlation for the solubility at 35 °C, 50 °C and 70 °C. While at 35 °C the correlation shows good agreements with experimental data, at higher temperatures the correlation increasingly underestimates the solubility of MgSO₃ with increasing MgSO₄ content.

![Figure 4. Solubility of MgSO₃ hexahydrate over MgSO₄ content at different temperatures [2,6,10].](image)

Figure 5. Solubility of MgSO₃ trihydrate over MgSO₄ content at different temperatures [2,6].

![Figure 5. Solubility of MgSO₃ trihydrate over MgSO₄ content at different temperatures [2,6].](image)
2.2. Calcium Sulfite (CaSO₃)

Equation (9) shows the solution equilibrium of CaSO₃ in water:

\[
\text{CaSO}_3 (s) + x \times \text{H}_2\text{O (aq)} \leftrightarrow \text{Ca}^{2+} (aq) + \text{SO}_3^{2-} (aq) + x \times \text{H}_2\text{O (aq)} \quad (9)
\]

Lutz states in the IUPAC solubility series that CaSO₃ precipitates primarily as hemihydrate (CaSO₃·1/2H₂O). The existence of dihydrate (CaSO₃·2H₂O) and tetrahydrate (CaSO₃·4H₂O) was also reported but not confirmed for the CaSO₃·H₂O system [2].

2.2.1. Solubility of CaSO₃ Hydrates in Water

The solubility data of CaSO₃ in the literature are scarce and existing data scatter over a wide range. Lutz evaluated in the IUPAC solubility several studies found in the literature [2]. Based on the evaluated data, Lutz recommends a solubility value of 0.0054 g/100 g of water at 25 °C. However, this value comes with a deviation of ±0.0012 g/100 g, which corresponds to around 22%. Lutz explains this strong scatter with the existence of different modifications of CaSO₃·1/2H₂O and its tendency to form supersaturated solutions [2].

Figure 6 shows the literature data of Bobrovnik and Kotelnikova and van der Linden, which were identified as the most accurate by Lutz, as well as the newer data of Malghe and Kumar [2,12–14].

![Figure 6. Solubility of CaSO₃ in water [2,12–14].](image)

The original data reported by Van Der Linden give the solubility for CaSO₃ dihydrate [14]. Due to the conclusion that the stable form is the hemihydrate, the solubility for hemihydrate is given in the IUPAC solubility series as calculated values based on the data reported by Van der Linden [2]. All data show a decrease in solubility with increasing temperature. The data from Malghe and Kumar strongly deviate from other literature data and greatly extend the deviation stated by Lutz. As the study does not specify the form of the analyzed CaSO₃ and due to the strong discrepancy, it is recommended to exclude these values for modeling purposes.
Lutz was able to correlate the literature data from Bobrovnik and Kotelnikova and van der Linden using the following equation with $S$ as the solubility in mol/K and $T$ as the temperature in Kelvin [2]:

$$\log S = -15.367 - \frac{1155.67}{T} - 3.290 \log T$$  \hspace{1cm} (10)$$

The plot of this correlation in Figure 6 shows good agreement with the literature data when excluding the data by Malghe and Kumar [13].

2.2.2. Influence of SO\(_2\) on Solubility of CaSO\(_3\) Hydrates

As for the MgSO\(_3\)-SO\(_2\)-H\(_2\)O system, the SO\(_2\) content also has an increasing effect on the solubility of CaSO\(_3\) [2]. Figure 7 shows the solubility of CaSO\(_3\) over the total SO\(_2\) content in the solution at 25 °C.

![Figure 7. Solubility of CaSO\(_3\) over total SO\(_2\) content in the solution [2,11].](image)

The data from Kuzminykh and Babushkina in 1956 are taken from the IUPAC solubility data series [2]. Lutz recommends describing the change in solubility with the presence of SO\(_2\) by following correlation with $S$ being the Solubility of CaSO\(_3\) in mol/kg and $b$ the molality of SO\(_2\) in mol/kg.

$$S_{\text{CaSO}_3} = 0.460 \times b_{\text{SO}_2} - 0.026 \times b^2_{\text{SO}_2}$$  \hspace{1cm} (11)$$

Figure 7 shows the applicability of this correlation for an SO\(_2\) content up to 10 g per 100 g water. For higher SO\(_2\) contents, the correlation slightly overestimates the solubility compared to the data from Conrad and Brice.

As for MgSO\(_3\), the increasing solubility with increasing SO\(_2\) content can be explained with the formation of Ca(HSO\(_3\))\(_2\).

2.2.3. Influence of CaSO\(_4\) on Solubility of CaSO\(_3\) Hydrates

CaSO\(_4\) has a decreasing effect on the solubility of CaSO\(_3\) [2]. Figure 8 shows solubility data of CaSO\(_3\) in water and in solution, which is saturated with CaSO\(_4\) over temperature.
2.2.3. Influence of CaSO₄ on Solubility of CaSO₃ Hydrates

CaSO₄ has a decreasing effect on the solubility of CaSO₃ [2]. Figure 8 shows solubility data of CaSO₃ in water and in solution, which is saturated with CaSO₄ over temperature.

Figure 8. Solubility of CaSO₃ in water and in CaSO₄ saturated solution [2,14,15].

All reported data show a significant decrease in the solubility of CaSO₃ in a solution, which is saturated with CaSO₄ compared to the solubility in water. The effect of decreasing solubility is on average around −58% and maximum −75%. Unlike for MgSO₃, there are no data reported, which analyze the effect of different sulfate concentrations on the solubility of CaSO₃.

2.3. Magnesium Sulfate (MgSO₄)

Equation (12) shows the solution equilibrium of MgSO₄:

\[
\text{MgSO}_4 (s) + x \times \text{H}_2\text{O (aq)} \leftrightarrow \text{Mg}^{2+} (\text{aq}) + \text{SO}_4^{2-} (\text{aq}) + x \times \text{H}_2\text{O (aq)} \quad (12)
\]

Many studies have examined the stability of different hydrate forms of MgSO₄ [16–20]. Following the study by Li et al. MgSO₄ exists stably as kieserite (MgSO₄·H₂O) and hexahydrate (MgSO₄·6H₂O) at 50 °C and only as kieserite at 75 °C in the MgCl₂-MgSO₄-H₂O system [18]. Starkyite (MgSO₄·4H₂O) was recognized as metastable form at both temperatures and pentahydrate (MgSO₄·5H₂O) as metastable form at 50 °C. In a very recent study, Dongdong et al. have developed a thermodynamic model to predict the thermodynamic behavior of the Mg(OH)₂-MgSO₄-H₂O system. The model defines heptahydrate (MgSO₄·7H₂O) as stable form at temperatures lower than 45.85 °C, hexahydrate for the temperature range of around 45.85 to 71.85 °C and kieserite for temperatures higher than 71.85 °C [20]. A solubility diagram of the MgSO₄-H₂O system presented by Steiger et al. supports this observation giving similar temperature windows for the existence of heptahydrate, hexahydrate and kieserite as stable hydrate forms of MgSO₄ [17]. Nevertheless, several metastable hydrate forms, such as starkyite or pentahydrate, may coexist in this temperature range [16–18] and different studies give partially contradictory new insights in the complicated reaction system [18].

Solubility of MgSO₄ Hydrates in Water

Figure 9 presents measured and correlated solubilities of the different hydrate forms over temperature.
All reported data show a significant decrease in the solubility of CaSO₃ in a solution, which is saturated with CaSO₄ compared to the solubility in water. The effect of decreasing solubility is on average around −58% and maximum −75%. Unlike for MgSO₃, there are no data reported, which analyze the effect of different sulfate concentrations on the solubility of CaSO₃.

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### 2.4. Calcium Sulfate (CaSO₄)

Equation (14) describes the solution equilibrium of CaSO₄ in water:

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\text{CaSO}_4 (s) + x \times \text{H}_2\text{O} (aq) \leftrightarrow \text{Ca}^{2+} (aq) + \text{SO}_{4}^{2-} (aq) + x \times \text{H}_2\text{O} (aq)
\]  

(14)

Several studies report three main forms of CaSO₄, which is hemihydrate (CaSO₄*1/2H₂O), dihydrate (CaSO₄*2H₂O), and anhydrite (CaSO₄) [25,26]. While dihydrate is recognized as the stable form at temperatures lower than 40 °C and anhydrite at higher temperatures, hemihydrate is a metastable form and can coexist at temperatures around 90 to 130 °C [27–29].

#### 2.4.1. Solubility of CaSO₄ Hydrates in Water

The solubility of the different CaSO₄ hydrates was studied by several researchers [25,28–33]. The data are summarized in Figure 10.

![Figure 9. Solubility of MgSO₄ in water [21–24].](image)

The solubility of MgSO₄ salts in water is almost by factor 100 higher than the solubility of MgSO₃ hydrates (compare Figures 2 and 9). Except for kieserite, the different hydrate forms show a similar solubility behavior. The data from Ting and McCabe report around 25% lower solubility than the other data. Otherwise, the data are in very good agreement with each other. The solubility of all hydrate forms except kieserite increases with increasing temperature. Apelblat and Manzurola correlated their data with the following equation with \( S \) being the Solubility in mol/kg and \( T \) being the temperature in K [23]:

\[
\ln S = 39.172 - \frac{2795.9}{T} - 5.0309 \ln T
\]  

(13)

This correlation describes the solubility of all hydrate forms up to a temperature of 70 °C well when excluding the data from Ting and McCabe (see Figure 9). At higher temperatures, the solubility decrease of kieserite reported by Robson needs to be taken into account and cannot be covered by the given correlation.

### 2.4. Calcium Sulfate (CaSO₄)

Equation (14) describes the solution equilibrium of CaSO₄ in water:

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\text{CaSO}_4 (s) + x \times \text{H}_2\text{O} (aq) \leftrightarrow \text{Ca}^{2+} (aq) + \text{SO}_{4}^{2-} (aq) + x \times \text{H}_2\text{O} (aq)
\]  

(14)

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This correlation describes the solubility of all hydrate forms up to a temperature of 70 °C well when excluding the data from Ting and McCabe (see Figure 9). At higher temperatures, the solubility decrease of kieserite reported by Robson needs to be taken into account and cannot be covered by the given correlation.

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\text{CaSO}_4 (s) + x \times \text{H}_2\text{O (aq)} \leftrightarrow \text{Ca}^{2+} (\text{aq}) + \text{SO}_4^{2-} (\text{aq}) + x \times \text{H}_2\text{O (aq)} \tag{14}
\]

Several studies report three main forms of CaSO\textsubscript{4}, which is hemihydrate (CaSO\textsubscript{4} \* \( \frac{1}{2} \) H\textsubscript{2}O), dihydrate (CaSO\textsubscript{4} \* 2 H\textsubscript{2}O), and anhydrite (CaSO\textsubscript{4}) [25,26]. While dihydrate is recognized as the stable form at temperatures lower than 40 °C and anhydrate at higher temperatures, hemihydrate is a metastable form and can coexist at temperatures around 90 to 130 °C [27–29].

2.4.1. Solubility of CaSO\textsubscript{4} Hydrates in Water

The solubility of the different CaSO\textsubscript{4} hydrates was studied by several researchers [25,28–33]. The data are summarized in Figure 10.

![Figure 10. Solubility of CaSO\textsubscript{4} in water [25,28–33].](image_url)

The newer data are in good agreement with older data, which indicates good accuracy of the data. The solubility curves are clearly distinguishable between the three different hydrate forms. While the solubility of dihydrate increases with temperature in the stable window up to 40 °C, a further increase in temperature leads to a decrease in solubility for all hydrate forms. The phenomenon that the solubility of dihydrate starts decreasing at around 40 °C can be explained thermodynamically with the change of the sign of the heat of solution [31].

2.4.2. Influence of Mg\textsuperscript{2+} on Solubility of CaSO\textsubscript{4} Hydrates

The presence of magnesium and calcium can influence each other’s solubility. Several authors have reported the association effect of magnesium, which increases the solubility of CaSO\textsubscript{4} with an increasing presence of magnesium cations as the cation associates the partial sulfate ion to form stable MgSO\textsubscript{4} [25,34]. As a consequence of the formation of MgSO\textsubscript{4} the solubility of CaSO\textsubscript{4} increases. Wu et al. studied the influence of magnesium chloride on the solubility of CaSO\textsubscript{4}. They report that at a MgCl\textsubscript{2} content of around 9 mol/kg the solubility of CaSO\textsubscript{4} dihydrate is around half the solubility at the same temperature in water [25].

2.5. Magnesium Hydroxide (Mg(OH)\textsubscript{2})

When describing the solubility of Mg(OH)\textsubscript{2} in an aqueous solution, two main equilibria need to be considered. One is the dissociation of Mg(OH)\textsubscript{2} and the other is the formation of the ion pair MgOH\textsuperscript{+}.

\[
\text{Mg(OH)}_2 (s) \leftrightarrow \text{Mg}^{2+} (\text{aq}) + 2\text{OH}^- (\text{aq}) \tag{15}
\]

\[
\text{Mg}^{2+} (\text{aq}) + \text{OH}^- (\text{aq}) = \text{MgOH}^+ (\text{aq}) \tag{16}
\]

Therefore the solubility of Mg(OH)\textsubscript{2} is a distinctive function of the pH value of the solution [3,35]. Scholz and Kahlert studied the pH dependence of the solubility of metal hydroxides and established an equation describing the solubility \( S_{\text{Mg(OH)}_2} \) as a function of pH, the solubility product \( K_{\text{sol, Mg(OH)}_2} \) and the autoprotolysis constant of water \( K_w \) [35]:

\[
\log S_{\text{Mg(OH)}_2} = \log K_{\text{sol, Mg(OH)}_2} + 2 \log K_w - 2 \text{pH} \tag{17}
\]
This equation is based on the consideration that formed OH\(^-\) ions are part of the autoprotolysis reaction of water and takes the following definitions into account [35]:

\[
S_{\text{Mg(OH)\textsubscript{2}}} = c_{\text{Mg}^{2+}}
\]

(18)

\[
K_{\text{sol, Mg(OH)\textsubscript{2}}} = c_{\text{Mg}^{2+}} \times c_{\text{OH}^-}^2
\]

(19)

\[
K_W = c_{\text{H}_3\text{O}^+} \times c_{\text{OH}^-}
\]

(20)

\[
\text{pH} = -\log c_{\text{H}_3\text{O}^+}
\]

(21)

Knowing the solubility product of Mg(OH)\(_2\) this equation allows an easy calculation at which pH value the precipitation of Mg(OH)\(_2\) starts at a given temperature. While a lower pH value is leading to a higher solubility, Mg(OH)\(_2\) is almost insoluble at neutral pH or higher.

**Solubility of Mg(OH)\(_2\) in Water**

Lambert and Clever evaluated comprehensively available data in the IUPAC solubility data series [3]. Figure 11 shows solubility data of Mg(OH)\(_2\) in water.

![Figure 11. Solubility of Mg(OH)\(_2\) in water [3,20,36–41].](image)

The data from Näsänen (1942), Travers and Nouvel (1929), and Lambert (1982) were taken from the IUPAC solubility data series [3]. Due to the low solubility, the direct measurement of a precise value is difficult. Therefore, several studies derived the solubility in water indirectly from the solubility product determined by measurements in a ternary system [3]. These values are designated as indirect determination in Figure 11. Literature data distinguish between active and inactive Mg(OH)\(_2\). Active Mg(OH)\(_2\) describes the amorphous form of Mg(OH)\(_2\) after precipitation or hydration of MgO. Aging leads to a thermodynamic stable form with a lower solubility described as inactive Mg(OH)\(_2\) [3]. Several studies focused on the solubility change from active to inactive Mg(OH)\(_2\) [36,37]. Although
there is a general trend visible that active Mg(OH)$_2$ has a higher solubility, the spread of data points at room temperature makes it impossible to derive a systematic trend [3]. While the direct measurements done by Busch show only a slight decrease of solubility with progressing aging, Hostetler observed a solubility decrease by almost 50% [36,37]. As the value for the active Mg(OH)$_2$ from Busch is taken after 8 h of equilibration time, the small decrease can be explained with an already progressed aging at this time.

While there are several studies analyzing the solubility at room temperature, there are only a few studies covering a wider temperature range. Travers and Nouvel performed direct measurements of the solubility in water, Lambert and Clever determined the solubility indirectly [3]. Lambert and Clever explain the difference between the values of these two studies with insufficient aging of the Mg(OH)$_2$ by Travers and Nouvel [3]. Correlating the literature data Lambert and Clever recommend the following equation to describe the tentative values for the solubility of Mg(OH)$_2$ in water as a function of temperature with $S$ being the solubility in mol/kg and $T$ the temperature in Kelvin [3]:

$$\ln S = 81.965 - \frac{3432.07}{T} - 13.893 \ln T \tag{22}$$

The plot of this correlation in Figure 11 shows a good agreement with experimental data for temperatures higher than 20 °C.

In a very recent study, Dongdong et al. developed several thermodynamic models to describe the Mg(OH)$_2$-H$_2$O system based on the CALPHAD methodology [20]. The model describes the thermodynamic properties of the system through the Gibbs free energy. Adjustable parameters allow the optimization of the model by fitting it to literature data. They were able to describe the system by fitting the adjustable parameters to solubility data described in the literature. However, they found that using the previously described literature data to fit the model leads to inconsistent thermodynamic results. Whereas a model using the solubility product given by McGee and Hostetler to complement the determination of the Gibbs energy equation showed consistency at least in the temperature window from 0 °C to 50 °C [20,42]. The solubility product reported by McGee and Hostetler shows only a small temperature dependency with $-\log(K) = 10.89$ at 10 °C and $-\log(K) = 11.10$ at 90 °C [42]. Especially at higher temperatures, the model based on these values shows a high deviation from solubility data found in the literature (see Figure 11) [20]. Dongdong et al. conclude that the limitations in modeling the Mg(OH)$_2$-H$_2$O system are due to the general lack of reliable experimental data of the solubility of Mg(OH)$_2$.

2.6. Calcium Hydroxide Ca(OH)$_2$

Equation (23) shows the solution equilibrium of Ca(OH)$_2$:

$$\text{Ca(OH)}_2 (s) \leftrightarrow \text{Ca}^{2+} (\text{aq}) + 2\text{OH}^- (\text{aq}) \tag{23}$$

Like Mg(OH)$_2$, the solubility of Ca(OH)$_2$ depends on the state of aging and the pH value of the solution. Following the study by Scholz and Kahlert, the pH dependency of the solubility can be expressed in the same way as for Mg(OH)$_2$ with the solubility product of Ca(OH)$_2$ respectively, leading to the following equation [35]:

$$\log S_{\text{Ca(OH})_2} = \log K_{\text{sol, Ca(OH})_2} + 2\log K_w - 2pH \tag{24}$$

The evaluation of solubility data of Ca(OH)$_2$ by Lambert and Clever revealed that the difference in solubility between fresh and aged Ca(OH)$_2$ decreased with increasing temperature and was in general small [3]. Which justifies the focus on the solubility of aged Ca(OH)$_2$ only.
Solubility of Ca(OH)$_2$ in Water

Figure 12 shows the solubility of Ca(OH)$_2$ over temperature. Except for the data of Yuan et al. all shown literature data were evaluated by Lambert and Clever in the IUPAC solubility data series [3].

![Figure 12. Solubility of Ca(OH)$_2$ in water [3,32,43–46].](image)

The data from Fratini (1945), Hedin (1955), and Komar et al. (1976) were taken from the IUPAC solubility series [3]. The newer and older data are in very good agreement with each other. The solubility is around 100 times lower than for Mg(OH)$_2$ and decreases with increasing temperatures.

Lambert and Clever were able to correlate the literature data using the following equation with $S$ being the solubility in mol/kg and $T$ the temperature in Kelvin [3]:

$$
\ln S = 86.1534 - \frac{3492.14}{T} - 13.7494 \ln T
$$

(25)

Also the younger experimental data of Yuan et al. fit the correlation very nicely, which confirms the applicability of that correlation [3,32].

3. Conclusions

Solubility data for MgSO$_3$, CaSO$_3$, MgSO$_4$, CaSO$_4$, Mg(OH)$_2$ and Ca(OH)$_2$ were summarized and reviewed to provide a solid base for modeling purposes.

To cover the precipitation of MgSO$_3$ the solubility of its hexa- and trihydrate needs to be taken into account. The existence of these hydrate forms depends on the process conditions. Available solubility data for both hydrates cover a temperature range of 0 to 100 °C and are in good agreement with each other. The inverse dependency on temperature of the two hydrate forms makes it necessary to critical review, which hydrate form occurs under the given conditions in the process prior to its modeling.
The solubility data of CaSO$_3$ are scarce, and only for a temperature range of 50 to 100 °C is more than one corresponding data source available. CaSO$_3$ precipitates as different hydrate forms. However, the solubility behavior of these hydrate forms does not differ apparently. A differentiated consideration of the single hydrate forms is therefore not required to model precipitation accurately.

Much data reports the influence of the sulfates MgSO$_4$ and CaSO$_4$ on MgSO$_3$ and CaSO$_3$ respectively. To describe the precipitation accurately, it is essential to include this influence into a process model.

Investigations on the precipitation of MgSO$_4$ report multiple existences of metastable hydrate forms varying with temperature and relative humidity and sluggish kinetics [16,17,19]. The available solubility data of MgSO$_4$ cover a temperature range of 0 to 200 °C. The available data for each single hydrate form are scarce. The solubility behavior of all studied hydrate forms except kieserite do not differ apparently. The available data imply that the different hydrate forms can be described together based on their combined data. The solubility of kieserite however shows an inverse temperature dependency and needs to be considered separately.

The precipitation and solubility of CaSO$_4$ are well studied. To cover the solubility behavior accurately, the hemihydrate, the monohydrate and the dihydrate need to be taken into account. For all hydrate forms, more than one data source is available for a temperature range of 0 to 100 °C. All available data are in very good agreement with each other.

Studies of the solubility of Mg(OH)$_2$ and Ca(OH)$_2$ show that at pH value lower than 7, the precipitation of the hydroxides can be disregarded when modeling an industrial process. A change to higher pH values, however, can cause heavy precipitation. Mg(OH)$_2$ is almost insoluble in water. The precise values of the solubility scatter at room temperature between around 0.75 × 10$^{-3}$ and 2 × 10$^{-3}$ g/100 g, partially explained by the solubility difference of active and inactive Mg(OH)$_2$. Only two data sources are available for a wider temperature range of up to 200 °C, which show a corresponding trend. The solubility of Ca(OH)$_2$ in water is well studied by many different researchers in a temperature range of 0 to 100 °C. All available data are in very good agreement with each other. For temperatures higher than 100 °C only one data set was found, which blends very well with the data for lower temperatures.

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